

1 MC Creight

Naive

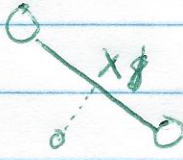
$$T_i : x[1 \dots n+1] \dots x[i \dots n+1]$$

T_1
 T_2
 T_3
 \dots

n strings to add

n search time

$$O(n^2)$$



MC Creight

$$\text{Let } x[i \dots n+1] = \text{head}(i) \text{tail}(i)$$

Longest $LCP(i, j)$ $j < i$

Parent already in the tree

How to find $\text{head}(i+1)$ from $\text{head}(i)$?

$$\text{head}(i) = x[i \dots i+h] \Rightarrow x[i+1 \dots i+h] \text{ prefix of } \text{head}(i+1)$$

Proof

$$h = 0$$

Trivial since $x[i+1 \dots i+0]$ is the empty string ✓

$$h > 0$$

$$\text{head}(i) = \boxed{a} y$$

$$\exists j : LCP(i, j) = ay$$

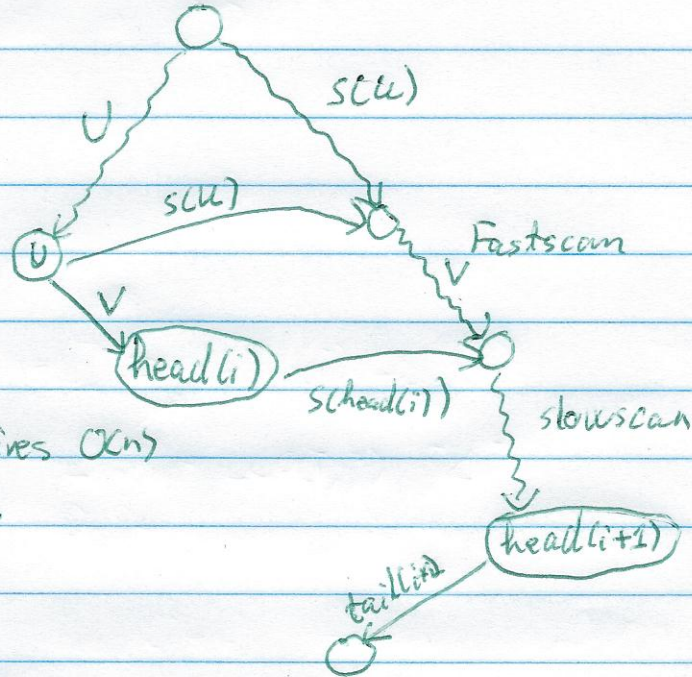
$$\Rightarrow y \text{ prefix of } LCP(i+1, j+1)$$

$$\Rightarrow y \text{ prefix of } \text{head}(i+1) \quad \checkmark$$

How it works

T_i invariants

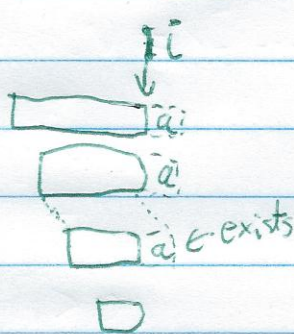
- non-terminal nodes have $SC(-)$
- except maybe $head(i)$



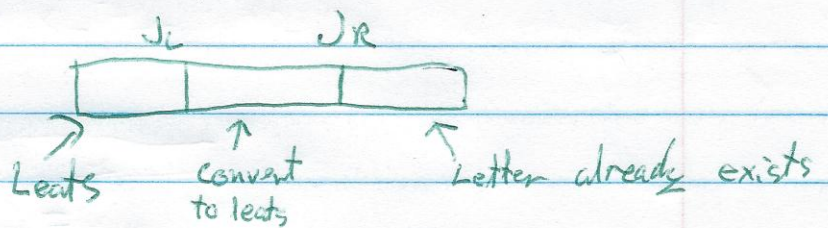
Optimization gives $O(n)$ running time.

Ukkonen

T_i



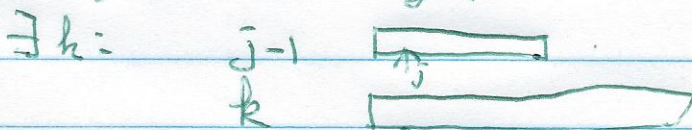
Trick: it leaf represent as (j, ∞) now free to add next letter



$j > 1$ leaf $\Rightarrow j-1$ leaf

Proof

Antag $j > 1$ leaf og $j-1$ not leaf



$\Rightarrow j > 1$ is leaf \Rightarrow contradiction.